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Section 3.2:

1 is called the multiplicative identity b/c $a \cdot 1 = a$. So multiplying by 1 doesn't change the value of a

ex1:
$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 \cdot 1 + 2 \cdot 0 & 1 \cdot 0 + 2 \cdot 1 \\ 3 \cdot 1 + 4 \cdot 0 & 3 \cdot 0 + 4 \cdot 1 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \leftarrow \text{same matrix comes out}$$

$2 \times 2 \quad 2 \times 2$

We call $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ the identity matrix = I_2

ex2:
$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 \cdot 1 + 2 \cdot 0 + 3 \cdot 0 & 1 \cdot 0 + 2 \cdot 1 + 3 \cdot 0 & 3 \cdot 1 \\ 4 \cdot 1 + 5 \cdot 0 + 6 \cdot 0 & 4 \cdot 0 + 5 \cdot 1 + 6 \cdot 0 & 4 \cdot 0 + 5 \cdot 0 + 6 \cdot 1 \\ 7 \cdot 1 + 8 \cdot 0 + 9 \cdot 0 & 7 \cdot 0 + 8 \cdot 1 + 9 \cdot 0 & 7 \cdot 0 + 8 \cdot 0 + 9 \cdot 1 \end{bmatrix}$$

$3 \times 3 \quad 3 \times 3$

$$= \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \leftarrow \text{We have the same as the original matrix output!}$$

We call $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ the identity matrix for 3 by 3 matrices. I_3

Example 10/Page 129:

The price per share for Wal-Mart (WMT), Target(TGT) and Costco(Cost) common stock at the close of trading on November 1st of 2007 and 2008 and 2009 are shown in the matrix A.

For 2007: we have three prices. For 2008, we again have three prices. For 2009, we again have three prices.

	<i>WMT</i>	<i>TGT</i>	<i>COST</i>
2007	$\begin{bmatrix} 42.16 & 56.58 & 63.17 \\ 54.54 & 39.24 & 56.03 \\ 50.03 & 49.17 & 57.75 \end{bmatrix}$		
2008			
2009			
		3×3	A

Kathleen and Shannon have each kept constant numbers of shares of each.

	<i>Kath.</i>	<i>Shannon</i>	
<i>WMT</i>	$\begin{bmatrix} 150 & 125 \\ 100 & 75 \\ 50 & 100 \end{bmatrix}$		B
<i>TGT</i>			
<i>COST</i>			
		3×2	

$$AB = \begin{bmatrix} 42.16 & 56.58 & 63.17 \\ 54.54 & 39.24 & 56.03 \\ 50.03 & 49.17 & 57.75 \end{bmatrix} \begin{bmatrix} 150 & 125 \\ 100 & 75 \\ 50 & 100 \end{bmatrix} = \begin{bmatrix} 42.16 \cdot 150 + 56.58 \cdot 100 + 63.17 \cdot 50 & 42.16 \cdot 125 + 56.58 \cdot 75 + 63.17 \cdot 100 \\ 54.54 \cdot 150 + 39.24 \cdot 100 + 56.03 \cdot 50 & 54.54 \cdot 125 + 39.24 \cdot 75 + 56.03 \cdot 100 \\ 50.03 \cdot 150 + 49.17 \cdot 100 + 57.75 \cdot 50 & 50.03 \cdot 125 + 49.17 \cdot 75 + 57.75 \cdot 100 \end{bmatrix}$$

<i>Wal</i>	<i>Tar</i>	<i>Cos</i>	<i>K</i>	<i>S</i>	2007	$\begin{bmatrix} \$15,140.50 & \$15,830.50 \\ \$14,906.50 & \$15,363.50 \\ \$15,309.00 & \$15,716.50 \end{bmatrix}$
					2008	
					2009	
			<i>K</i>	<i>S</i>		

Focus on (for no reason) \$15, 830.50 : this is the total investment value for Shannon in 2007.

Example 11/Page 130:

$$A = \begin{bmatrix} & \text{JJC} & \text{CSU} \\ \text{Margareta} & 12 & 3 \\ \text{Emilio} & 9 & 6 \end{bmatrix}$$

$$B = \begin{bmatrix} & \text{cost per credit hour} \\ \text{JJC} & 73 \\ \text{CSU} & 189 \end{bmatrix}$$

credit hours at Chicago State and Joliet Junior College

cost per credit hour for each university!

$$A = \begin{bmatrix} 12 & 3 \\ 9 & 6 \end{bmatrix}$$

$$B = \begin{bmatrix} 73 \\ 189 \end{bmatrix}$$

2×1

2by2

inside numbers are same, so we can multiply. Result will be 2 by 1 according to the outside numbers.

$$AB = \begin{bmatrix} 12 & 3 \\ 9 & 6 \end{bmatrix} \begin{bmatrix} 73 \\ 189 \end{bmatrix} = \begin{bmatrix} 12 \cdot 73 + 3 \cdot 189 \\ 9 \cdot 73 + 6 \cdot 189 \end{bmatrix} = \begin{bmatrix} 1443 \\ 1791 \end{bmatrix}$$

The 1443 is Margareta's cost to take her 15 credit hours.

The 1791 is Emilio's cost to take his 15 credit hours.

Question 1 Homework:

Table:

A brass maker makes three different types of wholesale brass blocks from copper and zinc according to the following table:

Brass Blends

	High Brass	Muntz Metal	Gilding Metal
Copper	65%	60%	95%
Zinc	35%	40%	5%

100%	100%	100%	not part of matrix
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(a) Make a 2 by 3 matrix B that contains the blending information in decimal form:

$$B = \begin{pmatrix} 0.65 & 0.60 & 0.95 \\ 0.35 & 0.40 & 0.05 \end{pmatrix} \quad 2 \times 3$$

(b) Plant 1 needs 8 High Brass, 3 Muntz Metal and 26 Gilding metal (in 1000's of lbs)

Plant 2 needs 10 High Brass, 5 Muntz Metal, 32 Gilding metal (32=32,000 lbs of Gilding M)

So we need a 3 by 2 so rows and columns match for multiplication: (We don't want 2 by 3)

$$\begin{bmatrix} 8 & 10 \\ 3 & 5 \\ 26 & 32 \end{bmatrix}$$

(c) Find the matrix product to find each location's need for each type of metal:

Pl. 1 Pl.2 3×2

$$\begin{bmatrix} 0.65 \cdot 8 + 0.60 \cdot 3 + 0.95 \cdot 26 & 0.65 \cdot 10 + 0.60 \cdot 3 + 0.95 \cdot 26 \\ 0.35 \cdot 8 + 0.40 \cdot 3 + 0.05 \cdot 26 & 0.35 \cdot 10 + 0.40 \cdot 5 + 0.05 \cdot 32 \end{bmatrix}$$

$$\begin{matrix} \text{copper} \\ \text{zinc} \end{matrix} = \begin{bmatrix} 31.7 & 39.9 \\ 5.3 & 7.1 \end{bmatrix} \quad \text{(d) Zinc is $.96 per pound and the price of copper is \$3.26 per pound.}$$

each entry represents PL1 PL2
the demand

$$\text{Total cost of Plant 1 is : } 3.26 \cdot 31.7 \cdot 1000 + 0.96 \cdot 5.3 \cdot 1000 = \$108,430.00$$

$$\text{Total cost of Plant 2 is: } 3.26 \cdot 39.9 \cdot 1000 + 0.96 \cdot 7.1 \cdot 1000 = \$136,890.00$$

