

Make sure the homework for today gets done by 8:00 pm later today. If you have to, once you have your system, just use a website to solve the system for m and b. Wolfram Alpha Saying like "I tried one or twice..." nothing! Try 10 times.

System of linear Inequalities: (Page 176...)

(1) Is $(-3, -10)$ a solution of the system

$$\begin{cases} -4x + 2y < 4 \\ 2x + y > -10 \end{cases} \xrightarrow{\text{replace x and y}} \begin{cases} -4(-3) + 2(-10) < 4 \\ 2(-3) + (-10) > -10 \end{cases} \xrightarrow{\text{simplify each LHS}} \begin{cases} 12 - 20 < 4 \\ -6 - 10 > -10 \end{cases}$$

$$\xrightarrow{\text{finalize each LHS}} \begin{cases} -8 < 4 \leftarrow \text{true} \\ -16 > -10 \leftarrow \text{false} \end{cases} \xrightarrow{\text{since one false...the point } (-3, -10) \text{ does not solve the system!}}$$

For a point to be a solution it's got to make both inequalities true.

Graphing $2x + 3y \geq 6$

1 graph boundary line: $2x + 3y = 6$

$x = 0: 2 \cdot 0 + 3y = 6 \rightarrow 3y = 6 \rightarrow y = 2$
 $(0, 2)$

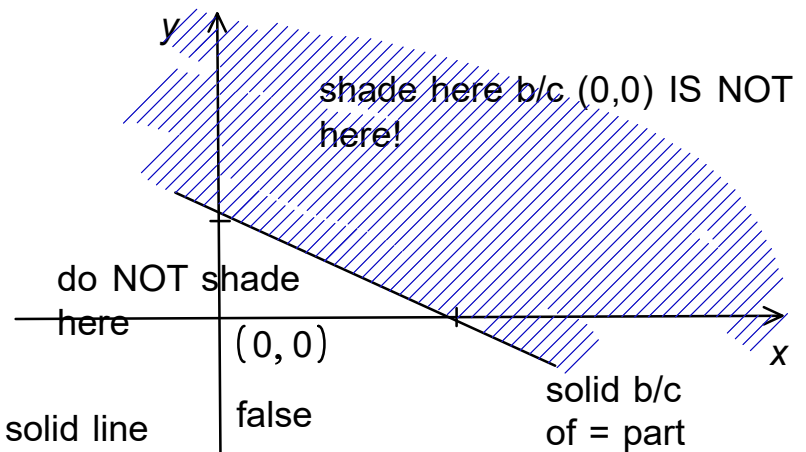
$y = 0: 2x + 3 \cdot 0 = 6 \rightarrow 2x = 6 \rightarrow x = 3$
 $(3, 0)$

Observe we have $> =$..b/c = is present, use solid line

B/c of $>$..do we shade above or below the line?

plug in $(0,0): 2 \cdot 0 + 3 \cdot 0 \geq 6$
 $0 + 0 \geq 6$
 $0 \geq 6$ false!

DO NOT SHADE WHERE $(0,0)$ is located!



Example of one inequality in two variables: x and y

Process: Pretend it's an equation so you can mark the boundary.

set $x=0$ and get y intercept.

set $y=0$ and get x intercept.

if inequality has \geq or \leq , use a solid line b/c of the = part

mark the intercepts and connect them with a line

if inequality has only $<$ or $>$, use a dashed line

where to shade? plug in $(0,0)$..if $(0,0)$ makes it true, shade in that region where $(0,0)$ is located.

if $(0,0)$ makes it false, shade on the other side of the line!

Let's practice graphing: $\begin{cases} 2x + y \leq 6 \\ x - y \geq 3 \end{cases}$

$2x + y \leq 6$ pretend it's $2x + y = 6$

$x = 0: y = 6 \rightarrow (0, 6)$

$y = 0: 2x = 6 \rightarrow x = 3 \rightarrow (3, 0)$

we have \leq .. use solid line

plug in $(0,0): 2 \cdot 0 + 0 \leq 6?$

$0 \leq 6$ true!

shade where $(0,0)$ is located!

Solution set will be the intersection of the two individually shaded parts.

Repeat steps above for each inequality on its own.

$x - y \geq 3$ becomes $x - y = 3$

$x = 0: 0 - y = 3 \rightarrow y = -3 \xrightarrow{\text{point}} (0, -3) \bullet$

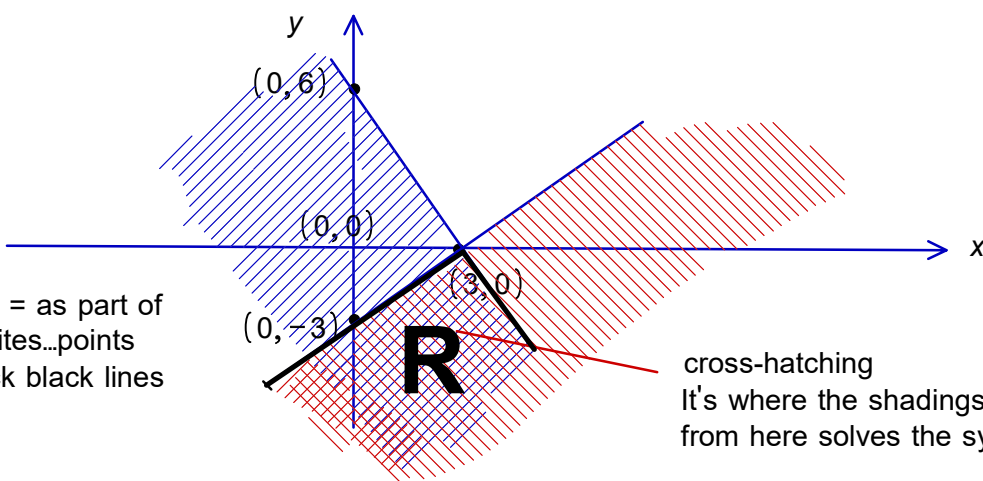
$y = 0: x - 0 = 3 \rightarrow x = 3 \rightarrow \text{point} = (3, 0)$

we have \geq .. use solid line

plug in $(0,0): 0 - 0 \geq 3$

$0 \geq 3$ false

so shade where $(0,0)$ IS NOT located!



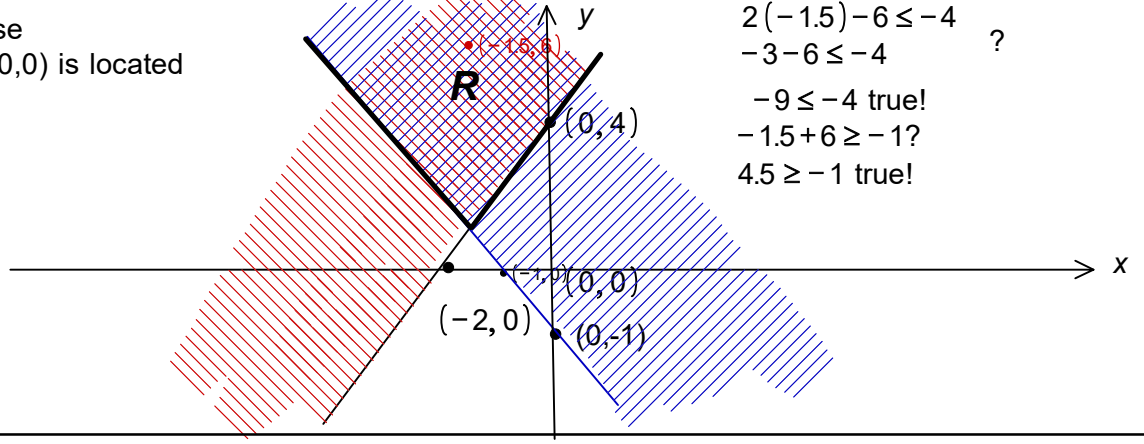
B/c we have = as part of both inequalities... points from the thick black lines also work!

cross-hatching
It's where the shadings overlap. Any point from here solves the system.

graph: $\begin{cases} 2x - y \leq -4 \\ x + y \geq -1 \end{cases}$
 $2x - y \leq -4$ becomes $2x - y = -4$
 $x = 0: -y = -4 \rightarrow y = 4 \xrightarrow{\text{point}} (0, 4)$
 $y = 0: 2x = -4 \rightarrow x = -2 \xrightarrow{\text{point}} (-2, 0)$
 b/c of the = in \leq , use a solid line
 plug in $(0, 0): 2 \cdot 0 - 0 \leq -4?$
 $0 \leq -4$ false
 so DO NOT shade where $(0, 0)$ is located

$x + y \geq -1$ becomes $x + y = -1$
 $x = 0: y = -1 \xrightarrow{\text{point}} (0, -1) \bullet$
 $y = 0: x + 0 = -1 \rightarrow x = -1 \xrightarrow{\text{point}} (-1, 0) \leftarrow$ fix this!!
 b/c of the = part of \geq , use a solid line
 plug in $(0, 0): 0 + 0 \geq -1?$
 $0 \geq -1?$ true
 shade where $(0, 0)$ is located!

Any point from R solves the system
 Any point from the thick black lines also solves the system.
 point in R: $(-1.5, 6)$
 $2(-1.5) - 6 \leq -4$?
 $-3 - 6 \leq -4$?
 $-9 \leq -4$ true!
 $-1.5 + 6 \geq -1?$
 $4.5 \geq -1$ true!



graph: $\begin{cases} -2x + y \leq -6 \\ 4x + 5y \geq 20 \end{cases}$
 $-2x + y = -6$
 $x = 0: y = -6 \xrightarrow{\text{point}} (0, -6)$
 $y = 0: -2x = -6 \xrightarrow{\text{solve for } x} x = 3 \xrightarrow{\text{point}} (3, 0)$
 b/c of the = part of \leq , use a solid line
 plug in $(0, 0): -2 \cdot 0 + 0 \leq -6?$
 $0 \leq -6?$ false
 so shade where $(0, 0)$ is NOT located!

$4x + 5y = 20$ (boundary line)
 $x = 0: 5y = 20 \xrightarrow{\text{divide by } 5} y = 4 \xrightarrow{\text{point}} (0, 4)$
 $y = 0: 4x = 20 \xrightarrow{\text{divide by } 4} x = 5 \xrightarrow{\text{point}} (5, 0)$
 b/c of the = part of \geq , use a solid line
 plug in $(0, 0): 4 \cdot 0 + 5 \cdot 0 \geq 20?$
 $0 + 0 \geq 20$
 $0 \geq 20$ false
 so shade where $(0, 0)$ is NOT located!

in older books...
 \geq was written as $> =$
 in older books \leq was written as $< =$

Since both inequalities have = present, the lines that bound the region R also solve the inequalities, so trace over them in bold black.

