

It's your job to send me a DETAILED list of any assignments you want to fix up. Everything must be wrapped up by the day of the final. After the final, I will not respond to anymore homework extension requests. If your grade in MyOpenM is far below 60, you will fail the class and have to do it again.

Section 6.1: Systems of Equations:

1. $\begin{cases} 2x+y=5 \\ 3x-2y=4 \end{cases}$, linear b/c it's x^1 and y^1 .

solve $2x+y=5$ for y : $y=5-2x$ (or x ..makes no difference, but y is easier)

replace y in equation 2 with $5-2x$:

$3x-2(5-2x)=4 \iff 3x-10+4x=4 \iff 7x-10=4$ ← replace y with $5-2x$...so method is called "substitution"

$7x-10+4x=4$

Since $x=2$, and $y=5-2x$:

$7x-10=4$

$y=5-2 \cdot 2=5-4=1$

$7x=14$

point: $(2, 1)$

$x=2$

2. solve $\begin{cases} x+y=4 \\ x-y=2 \end{cases}$ add the equations b/c we have $+y$ and $-y$: $x+y+x-y=4+2$ addition/elimination

$2x=6$

$x=6/2=3$

multiply equation 1 by -1 : $-x-y=-4$

solution point is $(3, 1)$

add equation 2: $x-y=2 \downarrow +$

$-2y=-2$

$y=-2/-2=1$

When we have $\begin{cases} ax+by=c \\ dx+ey=f \end{cases}$, x and y are the variables and each is raised to the 1st, so it's called a linear system.

substitution or addition/elimination

Non-Linear System: $\begin{cases} x^2-2y=25 \\ x^2+5y=25 \end{cases}$ non-linear b/c we have x^2

Multiply equation 1 by -1 (every single term) $-x^2+2y=-25$

Get x :

add equation 2: $+x^2+5y=25 \downarrow +$

replace y with 0 in equation 1:(or 2)

~~$0x^2$~~ $+7y=0$

$x^2-2 \cdot 0=25$

points are

$x^2=25$

$(+5, 0), (-5, 0)$

$7y=0$

$\sqrt{x^2} = \pm \sqrt{25}$

$y=0$

$x = \pm 5$

solve the system: $\begin{cases} x^2-2y=9 \\ x^2+5y=9 \end{cases} \implies$ multiply bottom by -1 : $-x^2-5y=-9$

$x^2-2y=9$

tally line

$-7y=0$

$y=0$

Replace y with 0 in bottom equation:

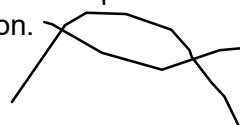
$x^2+5(0)=9$

$x^2=9$

$\sqrt{x^2} = \pm \sqrt{9}$

$x = \pm 3$

points: $(-3, 0), (3, 0)$. Each equation like $x^2-2y=9$ is a parabola, and so we have two points of intersection.



two points



no solutions



one point

Solve the system by graphing: $\begin{cases} y=(x+3)+4 \\ y-4=(x+3)^2 \end{cases}$

isolate y

$y=x+7$

$y=(x+3)^2+4$

graph each RHS!

A THING is not the same as the NAME by which its known.

graph $y = x + 7 \Rightarrow y = \frac{1}{1}x + 7$ (slope is 1/1 and y intercept is 7)

recall 1/1 is same as -1/-1

$$\frac{1}{1} = \frac{-1}{-1} = \mathbf{1}$$

$$\text{graph } y = (x+3)^2 + 4 = [x - (-3)]^2 + 4$$

parent parabola: $y = x^2$

basic parabola points:

$$(-1, 1) \rightarrow -3 \text{ on } x \rightarrow (-4, 1) \xrightarrow{\text{add 4 to } y} (-4, 5)$$

$$(0, 0) \rightarrow -3 \text{ on } x \rightarrow (-3, 0) \xrightarrow{\text{add 4 to } y} (-3, 4)$$

$$(1, 1) \rightarrow -3 \text{ on } x \rightarrow (-2, 1) \xrightarrow{\text{add 4 to } y} (-2, 5)$$

remember that $y = (x+3)^2 + 4$ is a parabola, so it should be curved! So solution points are $(-3, 4)$ and $(-2, 5)$

